## Diagonals of a Rhombus bisect opposite angles.



Diagonals of a parallelogram bisect each other.

$M$ is the midpoint of DB and $A C$

Kites and Trapezoids

## Trapezoids

A trapezoid is a quadrilateral with exactly one pair of parallel sides.

A trapezoid has 2 bases.
The bases are always the parallel sides.
The legs are always the nonparallel sides.


Show that ABCD is a trapezoid


If the legs of a trapezoid are congruent, then the trapezoid is an isosceles trapezoid.


If a trapezoid is isosceles, then each pair of base angles is congruent. (Thm 8.14)


A trapezoid is isosceles if and only if the diagonals are congruent. (Thm 8.16)


If a trapezoid has a pair of congruent base angles, then it is an isosceles trapezoid. (Thm 8.15)


This is an isosceles trapezoid. $m<A=95^{\circ}$ Find:
$m<B=$
$m<\mathrm{C}=$
$m<\mathrm{D}=$


The following quadrilaterals are trapezoids. Find the indicated values.


The midsegment of a trapezoid is a line that connects the midpoints of each leg.


The midsegment is parallel to both the bases.
The length of the midsegment is $1 / 2$ the sum of the lengths of the bases.
So $X Y=1 / 2(A D+B C)$.
Theorem 8.17

Find the length of the midsegment of this trapezoid given $\mathrm{BC}=12$ inches and $A D=28$.


Find the length of the midsegment of this trapezoid.


JKLM is a trapezoid. NP is the midsegment of this trapezoid.
Find ML


## Kites

A kite is a quadrilateral that has two pairs of consecutive congruent sides, but opposite sides are not congruent.


If a quadrilateral is a kite, then its diagonals are perpendicular. (Thm. 8.18)


If a quadrilateral is a kite, then exactly one pair of opposite angles are congruent. (Thm. 8.19)


Put an X in the box if the shape always has the given property.

| Property | Parallelogram | Rectangle | Rhombus | Square | Kite | Trapezoid |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| All sides are congruent |  |  |  |  |  |  |
| Both pairs of opposite sides are congruent |  |  |  |  |  |  |
| Both pairs of opposite sides are parallel |  |  |  |  |  |  |
| Exactly one pair of opposite sides are parallel |  |  |  |  |  |  |
| All angles are congruent |  |  |  |  |  |  |
| Exactly one pair of opposite angles are congruent |  |  |  |  |  |  |
| Diagonals are perpendicular |  |  |  |  |  |  |
| Diagonals are congruent |  |  |  |  |  |  |
| Diagonals bisect each other |  |  |  |  |  |  |

Put an X in the box if the shape always has the given property.

| Property | Parallelogram | Rectangle | Rhombus | Square | Kite | Trapezoid |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| All sides are congruent |  |  | $\mathbf{X}$ | $\mathbf{X}$ |  |  |
| Both pairs of opposite sides are congruent | $\mathbf{X}$ | $\mathbf{X}$ | $\mathbf{X}$ | $\mathbf{X}$ |  |  |
| Both pairs of opposite sides are parallel | $\mathbf{X}$ | $\mathbf{X}$ | $\mathbf{X}$ | $\mathbf{X}$ |  |  |
| Exactly one pair of opposite sides are parallel |  |  |  |  |  | $\mathbf{X}$ |
| All angles are congruent |  | $\mathbf{X}$ |  | $\mathbf{X}$ |  |  |
| Exactly one pair of opposite angles are congruent |  |  |  |  | $\mathbf{X}$ |  |
| Diagonals are perpendicular |  |  | $\mathbf{X}$ | $\mathbf{X}$ | $\mathbf{X}$ |  |
| Diagonals are congruent | $\mathbf{X}$ | $\mathbf{X}$ | $\mathbf{X}$ | $\mathbf{X}$ |  | $\mathbf{X}^{*}$ |
| Diagonals bisect each other | $\mathbf{X}$ | $\mathbf{X}$ | $\mathbf{X}$ | $\mathbf{X}$ |  |  |

## Pairs for Project

Sam, Charlene, and Victoria
Benji and Sarah
Heisu and Annie
Kevin, Selina, and Eleanor
Via and Poe
Juyeon and Ena
Lily and Christina

Section 8.5 - Kites and Trapezoids
Homework:
page 546: 7-15, 18-23, 25-29, 35, 36 ( 22 problems)
Draft your flow charts

